

FINANCIAL RESOURCE CONTRIBUTION TO PRODUCTION GROWTH AND RETURN ON PRODUCER'S CAPITAL

CONTRIBUCIÓN DE LOS RECURSOS FINANCIEROS AL CRECIMIENTO DE LA
PRODUCCIÓN Y RETORNO AL CAPITAL DE LOS PRODUCTORES

CONTRIBUIÇÃO DOS RECURSOS FINANCEIROS PARA O CRESCIMENTO DA
PRODUÇÃO E RETORNO AO CAPITAL DOS PRODUTORES

Daniel Villalobos Céspedes¹

Abstract

Financial resource contribution to production growth is a taboo issue in economic theory, especially if its source is the financial capital, which is part of the dynamic of any vigorous economy. Financial capital is a pivotal instrument of production growth due to the fact that its participation contributes to the process of transforming and transferring values from inputs to outputs. By doing so, financial capital encourages producers to generate not only outputs but also profit. Producers must transmute financial capital into financial resources in order to obtain output and profit. Therefore, the rate of interest becomes the way in which financial capital and producers get into the production process. This is to what this theoretical research is concerning.

Keywords: cost of production; loan; debt; resource; profit; interest

Resumen

La contribución de los recursos financieros al crecimiento de la producción es un tema tabú en la teoría económica, en especial si se trata del capital financiero, el cual es parte activa de la dinámica de una economía vigorosa. El capital financiero es un instrumento central del crecimiento económico en

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cuanto su participación contribuye en los procesos de transformación y transferencia de valor de los medios de producción al producto. Ese capital puede permitir a los empresarios generar productos y, por su medio, obtener ganancias. Para lograrlo, los productores transmutan el capital financiero en recursos financieros. La tasa de interés es un mecanismo que facilita al capital financiero y, a los productores, la incursión en procesos globales de producción.

Palabras claves: costo de producción; crédito; deuda; recurso; ganancia; tasa de interés

Resumo

A contribuição dos recursos financeiros para o crescimento da produção é um tema tabu na teoria econômica, especialmente em se tratando do capital financeiro, que é parte ativa da dinâmica de uma economia vigorosa. O capital financeiro é um instrumento central do crescimento econômico, na medida em que sua participação contribui para os processos de transformação e transferência de valor dos meios de produção para o produto. Esse capital pode permitir que os empresários gerem produtos e, através deste, obtenham lucros. Para conseguir isso, os produtores transmudam o capital financeiro em recursos financeiros. A taxa de juros é um mecanismo que facilita o capital financeiro e, para os produtores, a incursão em processos globais de produção.

Palavras-chave: custo de produção; crédito; dívida; recurso; lucro; taxa de juros.

Introduction

Production growth depends on various factors, many of which are challenging to explain. Economic theory uses facts that could be measured by different techniques, although this is not easy to conclude. What happens with financial capital and financial resources is where we must dig deeper into the concepts and facts. But to do so, we must make rational connections between concepts and between concepts and their fundamentals. This is the purpose of this theoretical research, analyzing concepts and their relations as they seem to occur in a real economy. We examine financial resource contribution to production growth and financial capital participation on profit.

This research is an advance on “Production Cost, Prices and Income of Firms” (Villalobos, [2015](#)). In the process of *transforming* inputs into outputs (Jehle & Reny, [2011](#), p. 126), input attributes are *transferred* into outputs. Money, as a coin or banknote, can be used to acquire resources, but

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itself alone is not a resource. Money as a concept can refer to anything, even those that can be a resource. As a means of transaction, money can facilitate the acquisition of goods and services of almost any kind. Some goods and services acquired by money are resources. Thus, money has the ability of acquire values as inputs, and by that it becomes capital.

What is called capital is anything (e.g. money) that can be used to generate any sort of benefit (e.g. economic profit g). By financial capital we understand certain amounts of assets, such as money, that could be reproduced by its profitable use no matter where it comes from (banks, stock market). This is possible if financial capital (credit, bonds, and shares) becomes a financial resource, because there is no way for financial capital to reproduce by itself. It is as a financial resource that financial capital (money or any other goods or services) given as loan ζ could make the global production process possible. Loans would not only facilitate the production process and production growth but also profit, and by this act, it would receive interest.

Interest is a ratio of profit, and because of this, financial resources would reflect the financial capital contribution to production growth. If an economy is a conjunction of resources, then money given-taken as a loan could be transmute into resources. A resource is anything useful for something else, especially to produce goods and services. However, it is not enough to produce it for sale; resources must be profitable. So, ζ becomes a financial resource, and as such, it seeks to participate in profit distribution. The rate of its participation is called the rate of interest \dot{i} , and so ζ and \dot{i} define debt C .

In a real economy, firms must deal with loans to acquire resources. In the production process, any resource assumes the form of production cost, so a loan becomes part of the cost as it is used to obtain resources. Credit is the way by which financial capital participates in the production process and also profit. The rate of interest is the means by which financial capital gets a fraction of profit as interest. Loans become financial resources in the hands of producers and through this, they contribute to production growth and generating profit.

Financial Resource on Production Cost

We call debt C and it is formulated as $C_t = F(\dot{i}, \zeta)$; $\zeta_t \leq C = F(\kappa K \bar{I}, \iota L; t)$, $\forall \{\kappa, \iota \in \mathbb{R}: (0 \leq \kappa, \iota \leq 1)\}$ and C represents the total value of the cost of production including fixed resource K , intermediate resource \bar{I} and labor L , and the rate of interest \dot{i} . So,

$$(1) C = (1 + \dot{i})\zeta \quad \text{then,} \quad C = \zeta + \dot{i}\zeta \quad \text{and} \quad (2) \dot{I} = C - \zeta = \dot{i}\zeta$$

For producers, ζ is the amount of money that corresponds to a part or total value of resources on production cost. Thus, $\zeta \leq C$ represents the magnitude of financial resources in the real value



of production cost. So, $\dot{C} = \dot{I}$ is not a cost but rather the quantity of interest (money) owed to financial resources for their contribution to production growth.

We will not complicate the computation of \dot{C}, \dot{I} by using compound interest due to the economy periodically paying a *quota* composite of \dot{I} *plus* a *portion* of \dot{C} . This quota may or may not imply proportional pays of \dot{I} and \dot{C} . Experience shows that financial capital charges a large proportion of \dot{I} instead of \dot{C} almost always from the beginning of \mathcal{C} . This is to say that financial capital charges interest on producers and also on loans to consumers, even before they generate profit as value. It is a fact that producers periodically require \dot{C} to finance the production process, so it is not easy to calculate how much producers pay on past-present debt. What we can suppose is that every so often (e.g. per month or year), the economy pays fractions of the value of production \dot{C}, \dot{I} to the financial sector.

To simplify our discussion in this research, we suppose that \dot{C}, \dot{I} correspond to the effective real value annually paid by the economy to the financial sector. So, \dot{C}, \dot{I} could vary from time to time depending on changes on \dot{C}, \dot{I} and the debt-term. Thus, to introduce \dot{C} to the production process as part of the value of production cost, we proceed as follows:

$$(3) c = \frac{\dot{C}}{C}$$

Equation (3) denotes the ratio of loan and thus the magnitude of loan in relation to the whole cost of production. Hence, c denotes the composition of the cost of production as a loan *plus* the producer's own capital (depreciation, profit). This means that c expresses the ability of the economy to sustain its production process. For this reason, it is necessary to analyze changes on C, \dot{C} ; thus, differentiating equation (3) obtains

$$dc = \frac{d\dot{C} C - \dot{C} dC}{C^2} = \frac{d\dot{C}}{C} - \frac{\dot{C} dC}{C^2}$$

Let $\hat{c} = \frac{dc}{c}$ be the rate of change on the loan amount and $\hat{c} = \frac{dC}{C}$ the rate of change on the cost of production, and by equation (3), we obtain

$$dc = c(\hat{c} - \hat{c})$$

$$\text{So, } \frac{dc}{c} = \hat{c} - \hat{c}$$

Let us call $\acute{c} = \frac{dc}{c}$ the rate of change in the ratio of loan. Therefore,

$$(4) \acute{c} = \hat{c} - \hat{c}$$



As result, \acute{c} will depend upon \hat{c} and on \hat{c} in opposite directions. So, the greater (lower) \hat{c} is than \hat{c} ceteris paribus (Figure 3), the greater (lower) the participation of financial resource on profit. If $\hat{c} = 0$, \acute{c} will be the opposite of \hat{c} , which is an indicator of the amount of profit that producers retain (Figure 1) or the contrary (Figure 2). In such a way, \hat{c} , \hat{c} , ceteris paribus, indicates the rate of participation of entrepreneurs on profit. For financial capital, we can say that its income is \acute{I} , while for producers it is just g .

But, we must keep in mind that participation on profit and contribution on profit have different connotations. For financial capital, its participation on profit is measured in terms of the rate of interest; meanwhile, for producers, it is computed in terms of the rate of profit. Contribution is measured here in relation to the value of production growth, which is possible only by producers. So, financial capital participates in profit because producers transform \acute{C} into a financial resource (into C), and as such it contributes to production growth. Of course, financial capital indirectly participates in production growth due to producers transforming loans into capital resources. But, if we discuss capital resources, we also talk of capital resource contribution.

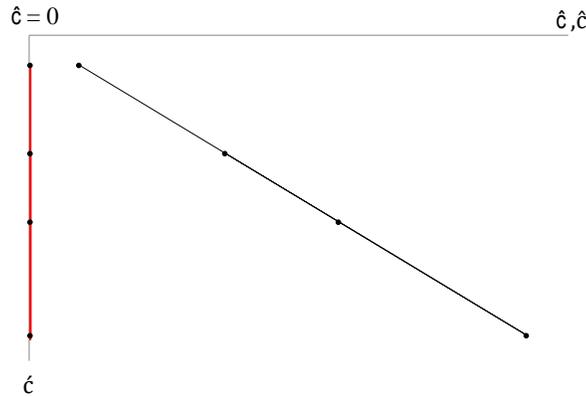


Figure 1. $\hat{c} = 0, \hat{c} > 0$. Source: Prepared by the author.

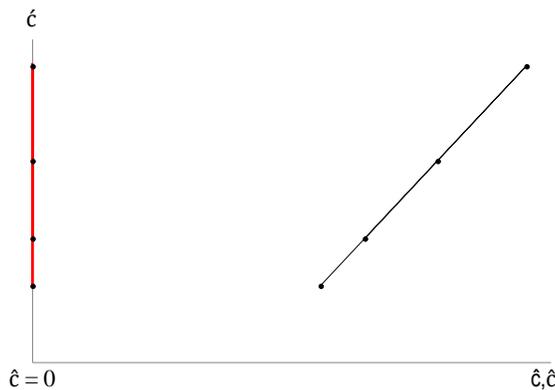


Figure 2. $\hat{c} = 0, \hat{c} > 0$. Source: Prepared by the author.



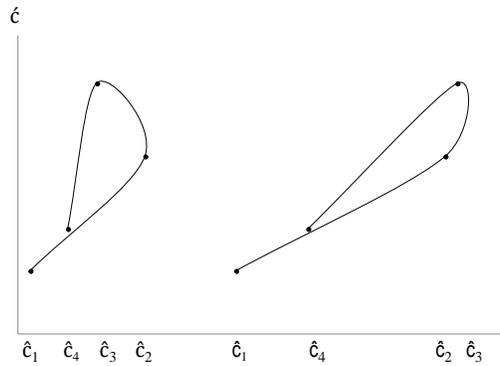


Figure 3. $(\hat{c} > \hat{c}) > 0$. Source: Prepared by the author.

By operating on equation (1) and substituting the result in equation (3), we get

$$c = \frac{\frac{c}{(1+i)}}{C} = \frac{c}{(1+i)C}$$

and by reorganizing it in function of C , we obtain

$$(5) C = \frac{c}{(1+i)c}$$

If C is the total value of the cost of production including fixed resource K , intermediate \bar{I} and labor L , the result is

$$C = \kappa(K + \bar{I}) + \iota L$$

This equation illustrates the composition of the real value of the cost of production, in which ζ is included if it exists. This is very important for the economy due to its ability to obtain loans effectively, and producer's own capital will rely on which kind of resources they invested. So,

$$(6) C = (1+i)cC = (1+i)c[\kappa(K + \bar{I}) + \iota L]$$

By this equation, the resources that will require financing by financial capital are determined.

Defining the *real* value of production VP as

$$(7) VP = r_J = r \frac{\kappa (K + \bar{I})}{\iota L}$$



and the average cost of production c is

$$(8) \quad c = \frac{C}{VP} = \frac{C}{rJ}$$

So, by equation (5),

$$(9) \quad c = \frac{\frac{c}{(1+i)c}}{rJ} = \frac{c}{(1+i)crJ}$$

and operating on the above equation, C is obtained which is equivalent to equation (5):

$$(10) \quad c r J = \frac{C}{(1+i)c} = C$$

In equation (10), it is perceived that C, ζ are given as part of VP denoted by crJ . Additionally, i plays a role on C through ζ , which will impact VP . By differentiating that equation, the result will be the change on C , taking into account all its components; that is to say,

$$dC = \frac{c(1+i)dC - [dc(1+i) + d\zeta]C}{[(1+i)c]^2} = \frac{dC}{(1+i)c} - C \left(\frac{dc}{c} + \frac{di}{1+i} \right)$$

Let $\dot{i} = \frac{di}{i}$ be the rate of change in the rate of interest and $\dot{c} = \frac{dc}{c}$ be the rate of change in *debt*, which will be influenced by changes in ζ, i and the debt-term. By replacing it and equation (10) in the previous equation, the result is

$$dC = C \left[\dot{c} - \left(\dot{c} + \dot{i} \frac{i}{1+i} \right) \right]$$

Let $\hat{c} = \frac{dC}{C}$ be the rate of cost. By reorganizing this result, we can rewrite that equation as

$$(11) \quad \hat{c} = \dot{c} - \left(\dot{c} + \dot{i} \frac{i}{1+i} \right)$$

Equation (11) expresses \hat{c} influenced by \dot{c} , which considers ζ as part of C and the amount of interest \dot{i} that the economy must pay, \dot{c} and the rate of change of the rate of interest $\dot{i} = \frac{di}{i}$.

Through equation (4), we can rewrite equation (11) as follows:

$$(12) \quad \hat{c} = \dot{c} - \left(\dot{c} - \hat{c} + \dot{i} \frac{i}{1+i} \right)$$

then, $\hat{c} = \dot{c} - \dot{c} + \hat{c} - \dot{i} \frac{i}{1+i}$



So, after simplifying,

$$0 = \check{c} - \hat{c} - \dot{i} \frac{1}{1+i} \quad \text{and thus, (13) } \check{c} = \hat{c} + \dot{i} \frac{1}{1+i}$$

Equation (13) denotes that \check{c} depends on \hat{c} and on the change of the rate of interest. If $\dot{i} = 0$, then $\check{c} = \hat{c}$, but $\dot{i} \neq 0$ would occur, ceteris paribus, due to changes in the rate of profit in the economy and in the rate of financial capital participation on profit, which defines the path of debt. Figures 4 and 5 illustrate two possibilities.

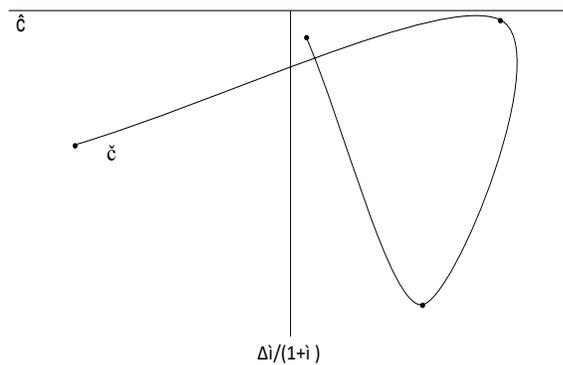


Figure 4. Path of debt due to \hat{c} and change in \dot{i} at different rates of profit ceteris paribus. Source: Prepared by the author.

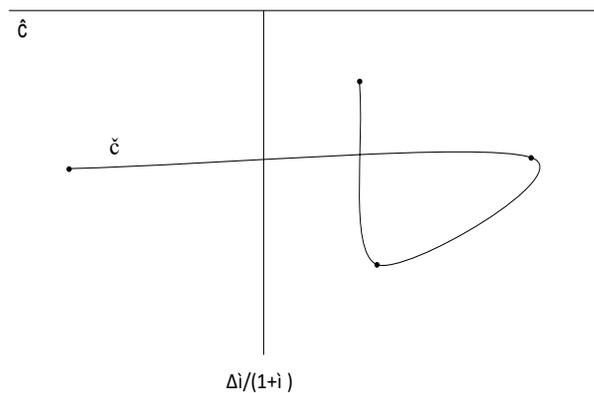


Figure 5. Path of debt due to \hat{c} and change in \dot{i} at different rates of profit and diminishing financial capital participation on profit ceteris paribus. Source: Prepared by the author.



Reasons of change in interest

By equation (10), we obtain

$$C = (1 + i) ccr \frac{\kappa K + \bar{I}}{L}$$

The quantity of interest \dot{I} paid (e.g. per annum) by the economy (firms, industries) is

$$C - ccr \frac{\kappa K + \bar{I}}{L} = \dot{c}cr \frac{\kappa K + \bar{I}}{L} = \dot{C} = \dot{I}$$

So,

$$(14) \dot{I} = \dot{c}cr \frac{\kappa K + \bar{I}}{L}$$

From equation (14), it is clear that \dot{I} , when it exists, is a result of the global process of production, where resources are combined to get a value of production. It also means that \dot{I} is a value that comes from VP every time \dot{C} is part of C . By the derivate of equation (14), we obtain

$$d\dot{I} = d\dot{c} cr \frac{\kappa K + \bar{I}}{L} + dc \dot{c}r \frac{\kappa K + \bar{I}}{L} + dc \dot{c}r \frac{\kappa K + \bar{I}}{L} + dr \dot{c}c \frac{\kappa K + \bar{I}}{L} + \dot{c}cr \frac{\kappa}{L} \left(\frac{L dI - I dL}{L^2} \right)$$

Where $I = K + \bar{I}$ and after simplifying, the following is obtained:

$$d\dot{I} = cr \frac{\kappa I}{L} [cd\dot{c} + \dot{c}dc + (\hat{c} - \tau)\dot{c}] + \dot{c}c \frac{\kappa I}{L} [rdc + cdr]$$

If $\dot{c} = \frac{dc}{c}$ is the rate of change in the rate of interest and $\dot{c} = \frac{dc}{c}$, then,

$$d\dot{I} = cr \frac{\kappa I}{L} [\dot{c}\dot{c} + \dot{c}\dot{c} + (\hat{c} - \tau)\dot{c}] + \dot{c}c \frac{\kappa I}{L} (\dot{c}c r + \hat{c}r c)$$

And

$$d\dot{I} = [\dot{c} + \dot{c} + (\hat{c} - \tau)] \dot{c}C + (\dot{c} + \hat{c}) \dot{c}C$$

After simplifying,

$$d\dot{I} = [\dot{c} + \dot{c} + (\hat{c} - \tau) + \dot{c} + \hat{c}] \dot{c}C$$



In addition, due to $\dot{I} = \dot{I}C$, then,

$$\frac{d\dot{I}}{\dot{I}} = \dot{\lambda} + \dot{c} + (\hat{i} - \tau) + \dot{c} + \hat{r}$$

Now, let $i = \frac{d\dot{I}}{\dot{I}}$ be the rate of change of \dot{I} , and substituting it in the above equation and by reorganizing it, we attain

$$i = \hat{r} + (\hat{i} - \tau) + \dot{c} + \dot{c} + \dot{\lambda}$$

After reorganizing, the result is

$$i = \lambda + \dot{c} + \dot{c} + \dot{\lambda}$$

This last equation expresses that the rate of change on \dot{I} will depend directly upon the rate of production growth λ , the rate of change of production costs, the rate of change of loans, and the rate of change in interest rate. It refers to how the economy gets \dot{I} from profit to pay it to financial capital. By replacing $\hat{c} = \lambda + \dot{c}$ and equation (4), we get

$$(15) i = \hat{c} + \dot{\lambda}$$

Equation (15) points out that the rate of change on \dot{I} is determined by the rate of change in loans and on the rate of change in interest rate. But this equation occults the fact that λ could influence the direction and magnitude of \dot{I} . So, *expectation* of financial capital on λ could establish a fundamental role in defining $\dot{\lambda}$. If by equation (4) $\hat{c}, \dot{\lambda} = 0$, then equation (15) will denote that producers will retain g .

Interest and profit on resource contribution

Profit is the prime inducement for investors to go into global production and financial activities in an economy. Profit g is measured by production value *minus* production cost value. So,

$$(16) g = VP - C$$

But gross profit is a result of every economic activity contribution to production growth by using productive resources. To get gross net producer's profit, we deduce from g the interest \dot{I} they will pay for financial resources. By equation (16) and $\dot{I} = \dot{I}C$, we obtain

$$g = VP - C - \dot{I}C = VP - (1 + \dot{I})C$$



And

$$(17) \dot{g} = rj[1 - (1 + i)c]$$

So, equation (17) denotes \dot{I} as featured in equation (14): the financial resource contribution to production growth. This fact is hidden by resource contribution to production growth expressed by λ . But, as we said before, this financial resource contribution to production growth reflects the financial capital participation on profit.

We can get the same result by a simpler proceeding, defining that

$$(18) \dot{i} = \frac{\dot{I}}{\dot{C}}$$

and by equation (14),

$$\dot{i} = \frac{\dot{i}ccrj}{\dot{C}}$$

then, after some manipulations,

$$(19) \dot{i}\dot{C} = \dot{i}ccrj = \dot{I}$$

Where \dot{I} was deduced by equations (2) and (14). If \dot{g} is the rate of profit calculated as

$$(20) \dot{g} = \frac{g}{C} = \frac{VP - C}{C}$$

By equations (7) and (10), we get

$$\dot{g} = \frac{\left[rj - \frac{C}{(1+i)c} \right]}{\frac{C}{(1+i)c}} = \frac{(1+i)crj}{C} - 1$$

and by substituting equation (9), we have

$$(21) \dot{g} = \frac{1}{c} - 1$$



The rate of profit and the rate of interest could not exist if capital as money did not get to transform into productive resource (Robinson, [1953-1954](#)). Capital is not as simple as any stock of things, like money, but rather those things that become production resources and by this on production cost. So, C is not a stock of resources but instead resource values used to be capitalized, and not just as simple capital. It is the nature of equation (20) to measure, relatively, profit resource contribution. But the motivation of equation (19) is to deduce how much profit corresponds to financial resources. Both rates result from the same process, but they have to be split up when profit is distributed between financial capital and producers.

By deducing equation (18) from equation (20), we get producer's net profit g in the economy:
(22) $g = \dot{g}C - \dot{i}C$

By operating on equation (3) and replacing its result in equation (22), the result is

$$(23) g = \dot{g}C - \dot{i}C = (\dot{g} - \dot{i})C = (\dot{g} - \dot{i}) cr$$

So, each portion of production cost value will get the same \dot{g} , and for this reason \dot{i} is just a fraction of \dot{g} . So, let \bar{i} be the coefficient as follows:

$$(24) \bar{i} = \frac{\dot{i}}{\dot{g}}$$

and

$$(25) \dot{i} = \bar{i}\dot{g}$$

Substituting equation (25) in equation (23), we obtain

$$(26) g = (\dot{g} - \bar{i}\dot{g})cr = \frac{I}{L} = \frac{\kappa I}{\iota L} (1 - \bar{i})\dot{g}cr = (1 - \bar{i})g$$

which is equivalent to equation (17).

Furthermore, by also substituting equation (20) in equation (25), the following is obtained:

$$(27) \dot{i} = \bar{i}\frac{g}{C}$$

By deriving equation (27), we find the change of \dot{i} due to changes in production cost and profit:

$$d\dot{i} = d\bar{i}\frac{g}{C} + \bar{i}\left(\frac{dgC - g dC}{C^2}\right)$$



By simplifying,

$$d\dot{i} = d\bar{i} \dot{g} + \bar{i} \left(\frac{dg}{C} - \frac{g}{C} \frac{dC}{C} \right)$$

Then,

$$d\dot{i} = d\bar{i} \dot{g} + \bar{i} \left(\frac{dg}{C} - \frac{g}{C} \frac{dC}{C} \right)$$

If $\hat{g} = \frac{dg}{g}$ is the rate of change on profit, then,

$$d\dot{i} = d\bar{i} \dot{g} + \bar{i} (\hat{g} \dot{g} - \dot{g} \hat{c})$$

Finally, let $\tilde{i} = \frac{d\bar{i}}{\bar{i}}$ the rate of change on the coefficient \bar{i} , so,

$$d\dot{i} = \tilde{i} \bar{i} \dot{g} + (\hat{g} - \hat{c}) \bar{i} \dot{g}$$

And

$$(28) \quad d\dot{i} = [\tilde{i} + (\hat{g} - \hat{c})] \bar{i} \dot{g}$$

The result is that the rate of interest will change due to changes in the rates of changes \tilde{i} , \hat{g} , \hat{c} . It is shown in equation (28) that, ceteris paribus, $\hat{c} > \hat{g} > \hat{c}$ will introduce changes on \dot{g} . It could motivate the financial sector to vary \bar{i} as a way of changing its participation on \dot{g} . In addition, it could happen as a result of changes in production growth. We already know that

$$\hat{c} = \hat{r} + (\hat{i} - \tau) + \dot{c}$$

So, replacing it in equation (28), we obtain

$$(29) \quad d\dot{i} = \bar{i} \dot{g} \left[\tilde{i} + [\hat{g} - [\hat{r} + (\hat{i} - \tau) + \dot{c}]] \right]$$

And now we can define the rate of change on the rate of interest by using equation (25) to get

$$\frac{d\dot{i}}{\dot{i}} = \tilde{i} + (\hat{g} - [\hat{r} + (\hat{i} - \tau) + \dot{c}])$$

As $\acute{i} = \frac{d\dot{i}}{\dot{i}}$ is the rate of change on the rate of interest, then,



$$(30) \dot{i} = \bar{i} + [\hat{g} - [\hat{r} + (\hat{i} - \tau) + \hat{c}]]$$

So, \dot{i} is also determined by production growth due to the financial capital expectation and the rate of cost. In the short-term, it is probably $\bar{i}, \hat{g} = 0$, which will be reflected in equation (30).

Return on producer's capital

Additionally, if producers are paying \dot{i} to financial resource C , it is clear that \dot{i} represents the opportunity cost \dot{I} for using its own capital as capital resource.² This is to say that producers will attain a net rate of profit \bar{g} . By deducing equation (18) or (19) from equation (21), we get

$$(31) \dot{g} = \left(\frac{1}{c} - 1 \right) - \dot{i}$$

By multiplying both sides of equation (31) by C , we get the producer's net profit \bar{g} as follows:

$$\bar{g} = \left[\left(\frac{1}{c} - 1 \right) - \dot{i} \right] C$$

Then, by equation (8),

$$\bar{g} = VP - C - \dot{i}C = VP - (1 + \dot{i})C$$

By replacing VP, C , we get

$$(32) \bar{g} = r_J - cr_J - \dot{i}r_J = r_J [1 - (1 + \dot{i})c]$$

Now we found in equation (32) that the interest \dot{I} owed to financial resource and the interest as opportunity cost \dot{I} appear as $\dot{i}cr_J$, so,

$$(33) \dot{I} = \dot{i}cr_J - \dot{i}cr_J = (1 - c)\dot{i}cr_J = (1 - c)\dot{i}C$$

To prove the result given by equation (33), we deduce equation (32) from equation (18) as follows:

$$\dot{I} = r_J [1 - (1 + \dot{i}c)c] - r_J [1 - (1 + \dot{i})c]$$

²Keynes (1936, p.40) assumed a different criterion for defining *user* and *supplementary cost*, and *normal profit* in the long-period, introducing the *interest cost* and the *third term* he called *risk-cost*.



By simplifying,

$$\dot{I} = r_J [1 - (1 + \dot{i}c) c - 1 + (1 + \dot{i}) c]$$

and then,

$$\dot{I} = r_J [\dot{i}c - \dot{i}cc]$$

Consequently,

$$\dot{I} = r_J [(1 - c)\dot{i}c]$$

and after rearranging that result,

$$\dot{I} = (1 - c) \dot{i}cr_J$$

Due to $C = cr_J$, we get equation (33) again.

Thus, the minimum return expected by producer's own capital is what they could receive from financial capital at \dot{i} .³ Minimum return can be estimated by operating on equation (33) as follows:

$$\dot{i} = \frac{\dot{I}}{(1 - c)C}$$

So, by equation (3), $\zeta = cC$, and replacing it in the previous equation we get

$$\dot{i} = \frac{\dot{I}}{C - \zeta}$$

Now let $\mathcal{C} = C - \zeta$ be the producer's own capital, so,

$$\dot{i} = \frac{\dot{I}}{\mathcal{C}}$$

and \dot{i} is the minimum rate of return expected for producers and is equal to the rate of interest. By operationalizing, we find the minimum return expectation for producers as follows:

³It is not an *equalizing rate* as Fischer (1930, p. 55) defined as *rate of return over cost* which it is but also an average rate of interest. However, we can state that \dot{i} measures the minimum return of profit expected by producers on their own capital. That is to say: $\dot{i} = \dot{g}$ then $\dot{i}C = \dot{g}C \therefore \dot{I} = \dot{g}$. If $\dot{i} < \dot{g}$ appropriate enough to their \dot{I} prospect, producers will probably wish to use loans. So, by comparing \dot{i}, \dot{g} , producers could decide on using credit and own capital or only their own capital.



$$(34) \dot{I} = iC$$

By deriving equation (34), we obtain the changes in return due to changes on i, C . So,

$$d\dot{I} = i dC + d\dot{i} C$$

Let $\epsilon = \frac{dC}{C}$ the rate of change on producer's own capital, and at the rate of change on the rate of interest \dot{i} , we have

$$d\dot{I} = i\epsilon C + \dot{i} C \quad \text{So,} \quad d\dot{I} = iC(\epsilon + \dot{i})$$

And by equation (34), we get

$$\frac{d\dot{I}}{\dot{I}} = \epsilon + \dot{i}$$

Then, let $\ddot{i} = \frac{d\dot{i}}{\dot{i}}$ be the rate of change on the rate of return expected by producers, and thus,

$$(35) \ddot{i} = \epsilon + \dot{i}$$

In equation (35), we show that the rate of change on the rate of return depends on the rate of change on the rate of producer's own capital and the rate of change on the rate of interest. This equation is the counterpart of equation (15) $\dot{i} = \hat{c} + \dot{i}$.

Let us see some extreme calculations as an academic matter; first, if $\dot{i}, \epsilon = 0$, then of course $\ddot{i} = 0$. Second, if $\epsilon = 0; \dot{i} \neq 0$, then $\ddot{i} = \dot{i}$. Third, if $\dot{i} = 0; \epsilon \neq 0$, then $\ddot{i} = \epsilon$. Between these two last points, some combinations appear to show \dot{i}, ϵ defining \ddot{i} . These arrangements will not necessarily illustrate straight or curved lines but rather a cyclical situation, depending on economic dynamic. If ϵ rises at a different \dot{i} , the expectation of the rate of return could be lower than \dot{i} and producers could be motivated to invest their own capital. This means that producers could have a lower opportunity cost investing their own capital over a loan. In a case like this, producers would retain a great amount of profit by using their own capital rather than loans.

By equalizing equations (35) and (15), by replacing $\dot{i} = \frac{d\dot{i}}{\dot{i}}$ in equation (35), we can illustrate different situations in an economy.

$$\ddot{i} = \epsilon + \frac{d\dot{i}}{\dot{i}}$$



And after operating on equation (15) and substituting the result in the previous equation, we get

$$(36) \ddot{i} = \epsilon + \frac{d\dot{i}}{i - \hat{c}}$$

Thus, the expectation of producers on its own capital will depend on changes to financial capital expectations on $\lambda, \dot{g}, \dot{i}$.

Supposing $\dot{i} = 0; \epsilon \neq 0$, ceteris paribus, during certain periods does mean that \dot{i} remains constant in that period. This also signifies in equation (25) that \bar{i}, \dot{g} stay constant, which at the same time means that by equation (30), no changes occur in the economy. But c could change at the constant \dot{i} and thus by equation (35), $\ddot{i} = \epsilon$. So, it is possible, ceteris paribus, for producers to use loans to finance maintaining or replacing K , for instance, at the regular \dot{i} . If, ceteris paribus, it happens ($\epsilon = 0; \dot{i} \neq 0$), then $\ddot{i} = \dot{i}$. If the economy is stable, financial capital could change their propensity \bar{i} on constant \dot{g} and so \bar{i} will change, as suggested by equations (25) and (30).

Conclusions

Financial capital is an amount of money that indirectly participates in production growth. As financial capital becomes a financial resource, it contributes to production growth and in the generation of profit. It is as a financial resource that financial capital participates in production cost. Interest rate is a ratio of the rate of profit and the means by which financial resource participates in profit. Financial resource contributes to production growth and thus in the generation of profit. Periodically, producers pay financial capital an amount of money as interest which is a part of profit. Interest is just a name that a portion of profit assumes when it must be paid to financial capital. Together, financial capital and interest becomes the producer's debt.

So, changes in production cost must reflect changes in loans by means of the rate of change on a loan. This rate is an indicator of the participation of financial resources and producers in production growth and profit. These facts are revealed by the value of production and the rate of debt growth. In the long run, the rate of change on interest will depend on the rate of production growth and also on the technical feasibility, technological feasibility, and financial capital propensity on profit. For these reasons, the rate of profit could change, but it is less probable than the rate of interest. It would be due to the fact that the rate of profit is also influenced by market prices and rivalry intensity. So, the rate of interest as a ratio of the rate of profit could not vary by changes in the rate of profit. This explains why the rate of return of producer's own capital could change from time to time.

We propose to have found different theoretical results with respect to those we know about harmonizing concepts and its fundamentals. Futures investigations must contribute to improving



this analysis on production growth and financial capital participation. So, this study would be a useful contribution to enrich on the economic theory debate.

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